Image Categorization and Semantic Segmentation using Scale-Optimized Textons

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Abstract
In computer vision research, a texton is a representative dense visual word for the bag-of-keypoints method. It has proven its effectiveness in categorizing materials and in generic object classes. Despite its success and popularity, no report describes a study that has tackled the problem of its scale optimization for given image data and associated object categories. We propose scale-optimized textons to learn the best scale for each object in a scene. We incorporate them into image categorization and semantic segmentation. Our textonization module produces a scale-optimized codebook of visual words. We approach the scale-optimization problem of textons using the scene-context scale in each image, which is the effective scale of local context to classify an image pixel in a scene. We perform the textonization process using a randomized decision forest, which is a powerful tool with high computational efficiency in vision applications. Results of our experiments using MSRC and VOC 2007 segmentation datasets demonstrate that our scale-optimized textons improve image categorization and segmentation performance.

Keywords: scale-optimized textons; image categorization; semantic segmentation; decision forest

1 Introduction
Automatically categorizing images has become increasingly important for image retrieval systems such as those for photo-sharing on web-sites. Current search engines offer meta-tags based on simple characteristics of images in a given large dataset. Smart devices and systems for image retrieval would become radically more intelligent and easy to use if a set of text labels to an image based on its visual content could be provided automatically. Image categorization is a means to perform image retrieval and it can be helpful in semantic segmentation and object recognition tasks. Additionally, it can enhance understanding of visual contents for easy browsing of web-sites. Moreover, it can develop convergence technologies for databases, data mining, and artificial intelligence applications.

Recently, image categorization frameworks have shown that dense sampling of visual words [19] and their combinations with image cues [5] can improve their performance significantly [21]. Textons [11] are promising representative dense visual words. Although early texton studies were limited to their exclusive emphasis on artificial texture patterns instead of natural images [35], recent studies have proven the effectiveness of textons for categorizing materials [27], various scenes [1], and generic object classes [32]. Using a bag-of-features model [5 25], the framework for using textons as visual words has become popular and has demonstrated its success in recent years [34]. Textons, unlike sparse image features such as SIFT [17] or HOG [6], are useful in both object segmentation and recognition because of their high density [22].
Figure 1: Example images of the 'cow' category on MSRC dataset. The objects have different scales in a large dataset such as large scale (a), middle scale (b), and small scale (c). Darker pixels correspond to the smaller scale. Because, scale-optimized textons include both scale and textural context in each image pixel, we can produce more discriminative features to recognize the object in a scene.

The major shortcoming of the bag-of-features model is that it discards the scale and the spatial layout of visual words, which engenders a daunting problem hindering segmentation and recognition. When a texton is used as a visual word, incorporation of the scale and the spatial layout becomes an important issue. First, many works have been presented to overcome the problem of the spatial layout \cite{15, 31, 9, 28, 29}. To learn the model of object classes with incorporating texture, spatial layout, and context information, Shotton et al. proposed a texture-layout filter in TextonBoost algorithm \cite{23}. Their filter can capture a textural context between texture and spatial layout using a boosted combination of texton features. The filter markedly improved the accuracy of segmentation and recognition.

Nevertheless, little attention has been devoted to discarded scale information for given image data and associated object categories. A large dataset has numerous scales of objects that are present in an image. As shown in Fig. 1 although objects might fall into the same category such as 'cow', they have different scales in a scene. Scale information of an object can be an important cue for recognizing the object in a scene, but report in the literature describes the incorporation of scale information into textons.

To address scale information and textons, we propose scale-optimized textons for image categorization and semantic segmentation. We use more discriminative bag-of-features by extracting scale-optimized textons in the textonization process. The scale-optimized texton can incorporate a texture-layout filter to capture the scale and textural context of the objects in a scene. We approach the scale-optimization problem of textons using the scene-context scale in each image pixel, i.e., the effective scale of local context to classify an image pixel in a scene \cite{12}. Our textonization process is first conducted using random forests \cite{3}, which have been shown to be computationally highly efficient, to generate base textons. We then extend the random forests into multi-scale texton forests to generate various textons with different scales. Furthermore, we estimate a scene-context scale using the proposed multi-scale texton forests \cite{13}. Finally, it is possible to extract the scale-optimized texton. In other words, a scale-optimized texton is a discriminative feature extracted from each image pixel in the best scale for the local
context, accordingly, the scale-optimized texton includes both semantic and scale information for local textural context.

Our scale-optimized textons can be combined with texture-layout filters to improve segmentation accuracy further. For image categorization, a histogram of the class distributions of scale-optimized textons is computed over the whole image. The histogram is combined with texture-layout filters for semantic segmentation. To assess our framework, we compare the accuracy of categorization and segmentation with that of the state-of-the-art [22] using MSRC21 and VOC 2007 segmentation datasets. Our results show that our method achieves better categorization and segmentation accuracy than those of the state-of-the-art using scale-optimized textons. The contribution of this work is the incorporation of scale information into textons as the textural context of the object to make them more discriminative. This report is the first describing method incorporates scale context into the textonization process.

This paper is organized as follows. In Section 2, we review related works on segmentation and recognition related to the spatial layout and scale information. Section 3 explains the textonization process to find the best scale of objects using scene-context scale. Section 4 describes how to combine scale-optimized textons of each category into the image categorization and segmentation module. Section 5 presents experimentally obtained results related to performance. The salient conclusions are presented in the final section.

2 Related work

Texton [11, 18, 27] is an efficient image representation used for both object segmentation and recognition. Densely discriminative textons facilitate pixel-wise segmentation [24] and image labeling [33]. Malik et al. [18] analyzed images into texton channels for image segmentation by mapping each pixel to the texton nearest to its vector of bank filter responses. They established a typical textonization process such as computing filter-banks, performing k-means clustering, and nearest-neighbor assignment, but it is quite time-consuming. To avoid time-consuming computations, Shotton et al. [22] proposed a fast and efficient textonization process using randomized decision trees.

These textonization processes can produce efficient and powerful textons for segmentation and recognition. When objects in the same category have various scales in a dataset, however, scale becomes an important factor to be considered. The multi-scale framework is commonly used to include scale information.

Grauman and Darrell [10] proposed a fast kernel function called the pyramid match using multi-resolution histograms. The pyramid match hierarchically measures similarity between histograms, which consist of sets of features extracted from the finest resolution to the coarsest one. The proposed kernel approximates the optimal partial matching by computing a weighted intersection over multi-resolution histograms for classification and regression tasks.

Wang and Wang [30] proposed a multiple scale learning framework to learn the best weights for each scale in the spatial pyramid matching [15]. The multiple-scale learning method can ascertain the optimal combination of base kernels constructed in different image scales for visual categorization.

Kivinen et al. [14] proposed a multi-scale graphical model for categorization of natural scenes. They developed a nonparametric Bayesian model, which captures an interesting qualitative structure in novel images using a multi-scale representation. The model based on a tree structure engenders a fast and accurate categorization performance.

As explained above, existing multi-scale approaches are developed in kernel-based learning or in a graphical model. Their focus is how to incorporate multi-scale information into the learning process using extracted image features. In contrast, our method directly incorporates scale information into the feature extraction module, i.e., the textonization process. Our scale-optimized textons have scale context...
Figure 2: **Dilatation of a region of interest according to scale space** \( k \) **and multi-scale texton forest.** Various sizes of image patches are used for node split function in the multi-scale texton forests (left). The multi-scale texton forest consists of several semantic texton forests [22] with various scale levels. Each semantic texton forest consists of randomized decision trees with the same scale level (right).

in themselves.

## 3 Scale-Optimized Textonization

Scale-optimized textons are obtainable using the scene-context scale in each image pixel. In this section, we explain our textonization process and how to optimize textons to include the best scale using multi-scale texton forests.

### 3.1 Multi-scale Texton Forests

We perform textonization processing using randomized decision trees to formulate multi-scale texton forests. The semantic texton forests proposed by Shotton *et al.* [22] are used to generate different scale levels to obtain multi-scale texton forests.

The multi-scale texton forests \( \mathcal{F} \) consist of several semantic texton forests with various scale levels \( \mathcal{F} = \{ \mathcal{F}_1, \mathcal{F}_2, ..., \mathcal{F}_s \} \) as shown in Fig. 2 where the scale level is \( k = (1, 2, 3, ..., s) \). Each semantic texton forest is a combination of randomized decision trees, each of which has a different set of image patches for its nodes. Split node functions for a randomized decision tree compute the values of raw pixels within an image patch \( p \). By increasing the size of image patches for split node functions, we can expand a semantic texton forest to multi-scale texton forests with different scales.

In the first scale level \( k = 1 \), an image patch \( p_1 \) covers whole pixels within a \((d \times d)\) size on which the split node functions for the first semantic texton forest \( \mathcal{F}_1 \) act. In the next scale level \( k = 2 \), the increased image patch \( p_2 \) covers the pixels within a \((2d \times 2d)\) size excluding the former image patch \( p_1 \). Therefore, the size of image patch \( p_k \) is increased to \((kd \times kd)\) pixels excluding the image patch \( p_{(k-1)} \) for the former scale level \((k-1)\) as shown in Fig. 2.

The combinations of raw pixels within image patches \( p_k \) for split node functions are generated randomly. We also increase the number of the candidates quadratically with respect to the scale level \( k \).

Randomized decision forests have been used in classifiers [2, 16] or clustering [20] with fast and powerful performance. Semantic texton forests [22] are used for both clustering and local classification.
To textonize an image, an image patch $p_k$ is passed down the multi-scale texton forest according to their scale level. We can obtain the class distributions $P_k(c|L_k)$ by averaging the local distributions over the leaf nodes $L_k = (l_1, l_2, ..., l_T)$ at scale $k$ as

$$P_k(c|L_k) = \frac{1}{T} \sum_{t=1}^{T} P_k(c|l_t),$$

where $c$ is a category label of a pixel and $T$ is the number of randomized decision trees in $\mathcal{F}_k$. Several class distributions in multi-scale texton forests exist as

$$P(c|L) = \{(P_1(c|L_1), P_2(c|L_2), ..., P_s(c|L_s))\}.$$

### 3.2 Scene-Context Scale

Scene-context plays an important role in segmentation and recognition [7]. When the scene-context is used on a per-pixel level, we can capture the local context in which image pixels carry semantic information within a region of interest. Some image pixels, however, have ambiguous features at a very local scale, because the color and texture of the local level have no capability of identifying the pixel class. Therefore, every image pixel has its available range to search for a local context in a scene.

The effective region size for a local context is designated as the scene-context scale [12]. Given the object presence and location in a scene, its scale is related to this range. It can be a strong cue for recognizing the objects in the scene. We can estimate the scene-context per image pixel and use the scene-context scale to find textons with the best scale using multi-scale texton forests.

The scene-context scale of each image pixel is obtained by computing the entropies of an image patch in the leaf nodes of each randomized decision forest. The confidence of each semantic texton forest is therefore computed by the entropies of the class distribution over the leaf nodes in $\mathcal{F}_k$. We regard the confidence as the criterion to find the scene-context scale. Because an object has different
Figure 4: **Clustering and classification results on MSRC segmentation dataset using multi-scale texton forests.** The multi-scale texton forest can generate different textons according to scale levels. (a) Input images. (b) Ground-truth images. (c) – (h) Clustering and classification results according to scale levels \( k = (1, 2, 3, 4, 5, 6) \). The results correspond to each scale level: \( k = 1: \) (c), \( k = 2: \) (d), \( k = 3: \) (e), \( k = 4: \) (f), \( k = 5: \) (g), and \( k = 6: \) (h).

scales depending on a scene, and because the scale of background/foreground appearing together in a scene might be independent of the object, we estimate the scene-context scale per pixel.

The scale level of the semantic textons forest with minimum entropy of the class distribution is chosen as the scene-context scale at each image pixel \( i \). We compute the entropy \( E_k(i) \) of image pixel \( i \) from the class distribution \( P_k(c|L_k) \) in \( \mathcal{F}_k \) as

\[
E_k(i) = -P_k(c|L_k) \times \log P_k(c|L_k).
\]  

(3)

Among all scale levels \( k = (1, 2, 3, \ldots, s) \), the best level \( k^* \) is chosen with minimum entropy as

\[
k^* = \arg\min_k \{ \mathcal{F}_k \{ E_k(i) \} \}.
\]  

(4)

The scene-context scale of an image pixel \( i \) is the instance \( k^* \) of the most likely scale among all scale levels.

### 3.3 Scale-Optimized Texton

Given an image pixel \( i \), the image patches \( p \) centered at pixel \( i \) are classified by descending each randomized decision tree. A randomized decision tree provides both a hierarchical tree structure such as a path from the root to a leaf and the node class distributions at the leaf. Based on training data, the class distributions can be estimated by averaging the local distributions in randomized decision trees.
A scale-optimized texton can be generated by computing the scene-context scale of each image pixel from multi-scale texton forests. Among multi-scale texton forests, a semantic texton forest $F_{k^*}$ is selected in the textonization process. The semantic texton forest $F_{k^*}$ has the instance $k^*$ of the most likely scene-context scale. We can define the texton generated by the semantic texton forest $F_{k^*}$ as our scale-optimized texton.

Our scale-optimized textonization process exploits the class distributions $P_{k^*}(c|L_{k^*})$ in the semantic texton forest $F_{k^*}$ with the scene-context scale $k^*$. These scale and textural information are used in the statistics of scale-optimized textons. By classifying a histogram consisting of the statistics of scale-optimized textons, we can obtain good performance for pixel-level classification. Additionally, we can improve the estimation of class distributions from training data, even if the training data perform no geometrical transformation in terms of scale and orientation.

4 Categorization and Segmentation

Scale-optimized textons are used in the bag-of-features model for image categorization and semantic segmentation. Once a scale-optimized texton is determined, we can calculate the class distributions of each image pixel using the scale-optimized texton. We produce a histogram consisting of class distributions computed across the whole image for image categorization. The histogram contains the scale and textural context using both the most likely category $c_i^* = \arg\max_c P_{k^*}(c_i|L_{k^*})$, and the most likely scene-context scale $k^* = \arg\min_k (F_k \{E_k(i)\})$.

However, because the bag-of-features model discards spatial layout, we use a simple grid window to learn the layout of scale and textural context automatically, as shown in the middle of Fig. 3. The grid window consists of nine sub-grids as shown in the right of Fig. 3: Top-Left (TL), Top-Center (TC), Top-Right (TR), Center-Left (CL), Center-Center (CC), Center-Right (CR), Bottom-Left (BL), Bottom-Center (BC), and Bottom-Right (BR). We concatenated the histograms from TL to BR. The histogram is used as input to a classifier to recognize object categories.

We adopt the non-linear support vector machine (SVM) to classify each category. Multi-class classification is performed with LibSVM trained using the one-versus-all rule: a classifier is learned to separate each class from the rest, and a test image is assigned the label of the classifier with the highest response.

When a histogram is created over a region of interest for each pixel, it is useful in pixel-wise semantic segmentation. To obtain more accurate segmentation performance, it is possible to combine with the texture layout file instead of our simple grid window. However, because the class distributions are extracted from scale-optimized textons, the results of the first clustering and classification guarantee good performance. We present the performance of clustering and classification in Section 5.1.

5 Experimental Results

This section presents experimentally obtained results for image categorization and segmentation using scale-optimized textons. We evaluated our algorithm using MSRC and challenging VOC 2007 segmentation datasets that include various objects such as building, cow, sheep, water, face, cat, road, and sky.

The MSRC dataset has 256 images for training, 257 images for test, and remaining 59 images for validation. The VOC 2007 segmentation dataset has 209 images for training, 210 images for test, and remaining 213 images for validation. We used standard training/validation data for training and used test data for our test.
5.1 Scale-Optimized Textonization

To assess the efficiency of the proposed scale-optimized textons, we compared the class classification accuracy with that achieved by the conventional semantic texton forests method [22] without using the scale-optimized texton.

We separately trained the semantic texton forests at different scale levels. To train the multi-scale texton forest, we prepared six scale levels $k = (1, 2, 3, 4, 5, 6)$. The initial image patch size was $(15 \times 15)$. Therefore, the size of image patches $p$ for the split function is $(15k \times 15k)$ at each scale level $k$. Each semantic texton forest $F_k$ had the following parameters, $T = 5$ trees, maximum depth $D = 10$, $400 \times 2^k$ feature and $10k$ threshold tests per split function, and 0.25 of the data per tree. Training a semantic texton forest took approximately $30 \times 2^k$ min on the MSRC dataset and $60 \times 2^k$ min on the VOC 2007 at each scale step.

**MSRC Dataset** [24] Fig. [4] presents results of clustering and class classification based on multi-scale texton forests. We visualized the most likely categories of each pixel. As shown in Fig. [4], a semantic texton forest has different local class distributions according to its scale. Regarding results of the first and second rows of Fig. [4] we notice that the more the scale level increases, the more the performance also increases. The image of the third row shows the roughest result in the largest scale level. Most
intriguingly of all, the fourth row’s image has different performance among categories according to the scale level: the ‘face’ is classified at the smallest scale, but the ‘body’ is classified at a larger scale. The image of the last row, shows good performance in the smallest scale as we expected. Results show that the scene-context scale is estimated per image pixel.

Fig. 5 shows a several scene-context scale image of the MSRC test dataset. Using the scene-context scale, we can obtain scale-optimized textons, and can infer the most likely category for each pixel as shown in Fig. 5(a). Then Fig. 5(b) shows results of the state-of-the-art [22] based on single-scale semantic texton forests. The single-scale semantic texton forest used the same parameter of the multi-scale texton forests with the first scale level $F_1$.

Clustering and class classification performance are measured as both the class average accuracy (average proportion of pixels correct in each category) and the global accuracy (total proportion of pixels correct) as shown in the bottom table of Fig. 5. The global classification accuracy without scale-optimized textons gives 50.2%, although that with using scale-optimized textons scale gives 53.0%. Particularly significant improvement is visible in most classes. For some classes such as trees or water, however, no improvement is apparent. This lack of benefit might derive from the fact that they have no influence on scale-optimized textons because of their strong textural property. Across the whole MSRC dataset, using the scale-optimized textons achieved a class average performance of 48.3%, which is greater than the 38.4% of (b), as shown in Fig. 5.

**VOC 2007 Segmentation Dataset** [8] Fig. 7 shows the results of our scale-optimized textonization. As presented in Fig. 7, a pixel-level classification based on the class distributions gives a good performance (13.7%), even if it does not cooperate with any spatial-layout information. Therefore, we can confirm that the proposed scale-optimized textons can be powerful and discriminative visual words for the bag-of-features model.

## 5.2 Categorization and Segmentation

As a result of image categorization, we obtained the accuracy of VOC 2007 and MSRC categories, as shown respectively in the last row of the table of Fig. 7 and the upper side of table in Fig. 6. For a non-linear SVM classifier, we compared the class average using a radial basis function (RBF) kernel and pyramid match kernel (PMK) [10] to the state-of-the-art [22]. We confirmed that the RBF kernel gives
Figure 7: **Result images of clustering and the class classification (upper) on VOC 2007.** The VOC 2007 contains 21 challenging categories including the background. The bottom table shows the accuracy of the clustering and the class classification and also image categorization (last row).

<table>
<thead>
<tr>
<th>Semantic Segmentation</th>
<th>cat</th>
<th>background</th>
<th>person</th>
<th>car</th>
<th>aeroplane</th>
<th>bicycle</th>
<th>bird</th>
<th>boat</th>
<th>bottle</th>
<th>bus</th>
<th>chair</th>
<th>cow</th>
<th>table</th>
<th>dog</th>
<th>horse</th>
<th>motorbike</th>
<th>person</th>
<th>plant</th>
<th>sheep</th>
<th>sofa</th>
<th>train</th>
<th>monitor</th>
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<tbody>
<tr>
<td>Scale-optimized textons</td>
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<td>2</td>
<td>9</td>
<td>15</td>
<td>19</td>
<td>14</td>
<td>14</td>
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<td>19</td>
<td>13</td>
<td>13</td>
<td>5</td>
<td>4</td>
<td>28</td>
<td>27</td>
<td>9</td>
<td>7</td>
<td>12</td>
<td></td>
<td>13.7</td>
</tr>
<tr>
<td>Broeks 2007 [7]</td>
<td>6</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>9</td>
<td>5</td>
<td>10</td>
<td>1</td>
<td>2</td>
<td>11</td>
<td>0</td>
<td>6</td>
<td>6</td>
<td>29</td>
<td>2</td>
<td>2</td>
<td>0</td>
<td>11</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
<td>8.5</td>
</tr>
<tr>
<td>INRIA normal 2007 [7]</td>
<td>1</td>
<td>2</td>
<td>8</td>
<td>2</td>
<td>52</td>
<td>0</td>
<td>12</td>
<td>6</td>
<td>4</td>
<td>0</td>
<td>18</td>
<td>4</td>
<td>0</td>
<td>4</td>
<td>29</td>
<td>0</td>
<td>6</td>
<td>0</td>
<td>10</td>
<td></td>
<td></td>
<td></td>
<td>7.7</td>
</tr>
<tr>
<td>Image categorization</td>
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<td>11</td>
<td></td>
<td>95.9</td>
</tr>
</tbody>
</table>

Improved results than the PMK. As might be apparent, the proposed method using the scale-optimized textons provides considerably better results than the selected state-of-the-art method. It shows improved performance for all categories.

To demonstrate the power of the scale-optimized textons as features for segmentation, we employed the joint boosting algorithm [25] to select discriminative features of the bag-of-features model. The semantic segmentation results for MSRC test data are shown at the bottom of Fig. 6. As might be readily apparent, the proposed segmentation algorithm improves the accuracy in the local classification process. In particular, classes with the result of noisy clustering such as water, car, bicycle, sign and road, show good performance in this process. We obtained segmentation results with global 65.2% and class average 59.8% using the bag-of-features model with scale-optimized textons.

We compared results obtained using the proposed method with those obtained using the state-of-the-art method in the table of Fig. 6. In fact, the results obtained from the state-of-the-art method are better than 58.6% in their paper [22], because they augmented the training data with image copies that are artificially transformed geometrically and photometrically. However, our experiments use no geometric transformations, or affine photometric transformations such as rotation, scaling, and left-right flipping.

Additionally, they separately run the categorization and segmentation algorithms and multiply the distributions with image-level prior (ILP) to emphasize the likely categories and to discourage unlikely categories using the results of image categorization. However, we exclude the ILP of image categorization results for all experiments. Nevertheless, across the whole dataset under the same experimental conditions, the proposed method achieved a class average performance of 59.8%, which is better than the 58.6% that was obtained using the state-of-the-art method.
6 Conclusion

This paper presented a method that incorporates scale information into textons as local textural context of the object to make them more discriminative. Differently from existing methods, our method directly incorporates scale information into the textonization process. By extending random forests into multi-scale texton forests, our method generates different textons in scale. Then, using the scene-context scale, it finds the scale-optimized texton, i.e., the texton with the best scale in each image pixel. Our experiments showed that using our scale-optimized textons improves the performance of image categorization and segmentation. It is expected that our scale-optimized textons will be combined with texture-layout filters [24] to improve segmentation accuracy further.

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References

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